



FKITMCMXIX

Sveučilište u Zagrebu  
Fakultet kemijskog  
inženjerstva i tehnologije



# VODIK – SKLADIŠTENJE, PRIMJENA

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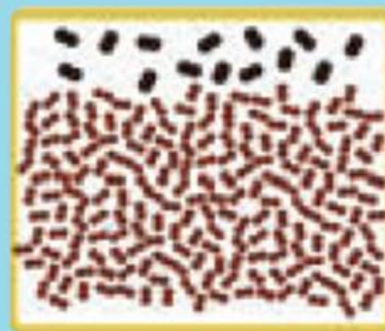
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# Skladištenje vodika

# Mogućnosti skladištenja

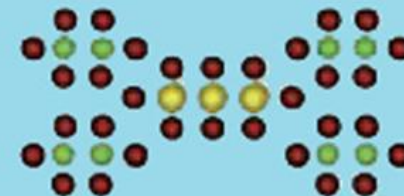
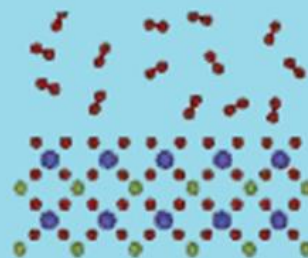
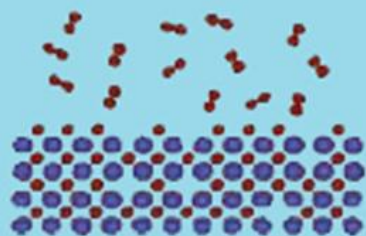
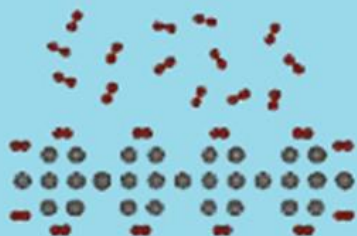


Plin pod pritiskom



Kriogena tekućina

- Atom vodika
- Molekula vodika



(a) površinska adsorpcija

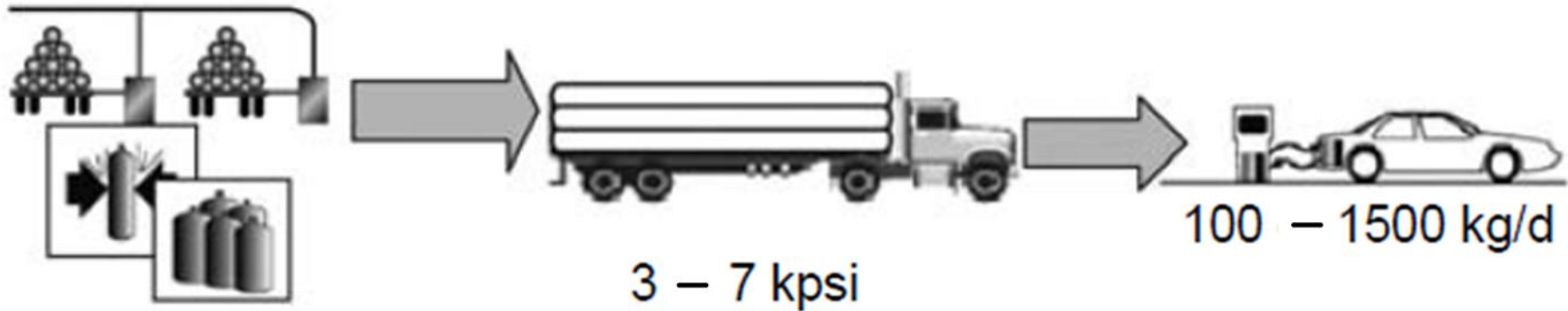
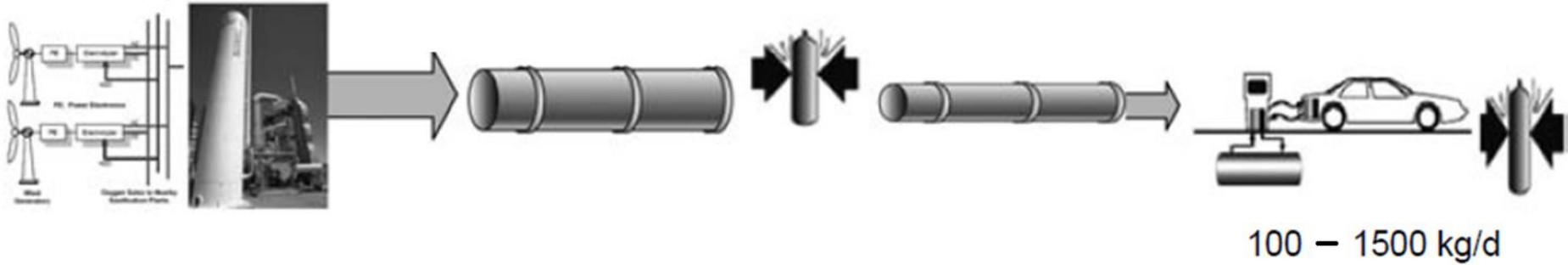
(b) metalni hidrid

(b) kompleksni hidrid

(c) kemijski hidrid

Povećanje gustoće

# Plinoviti vodik pod visokim tlakom $H_2$ (g)



3 – 7 kpsi

1 psi  $\approx$  64895 Pa

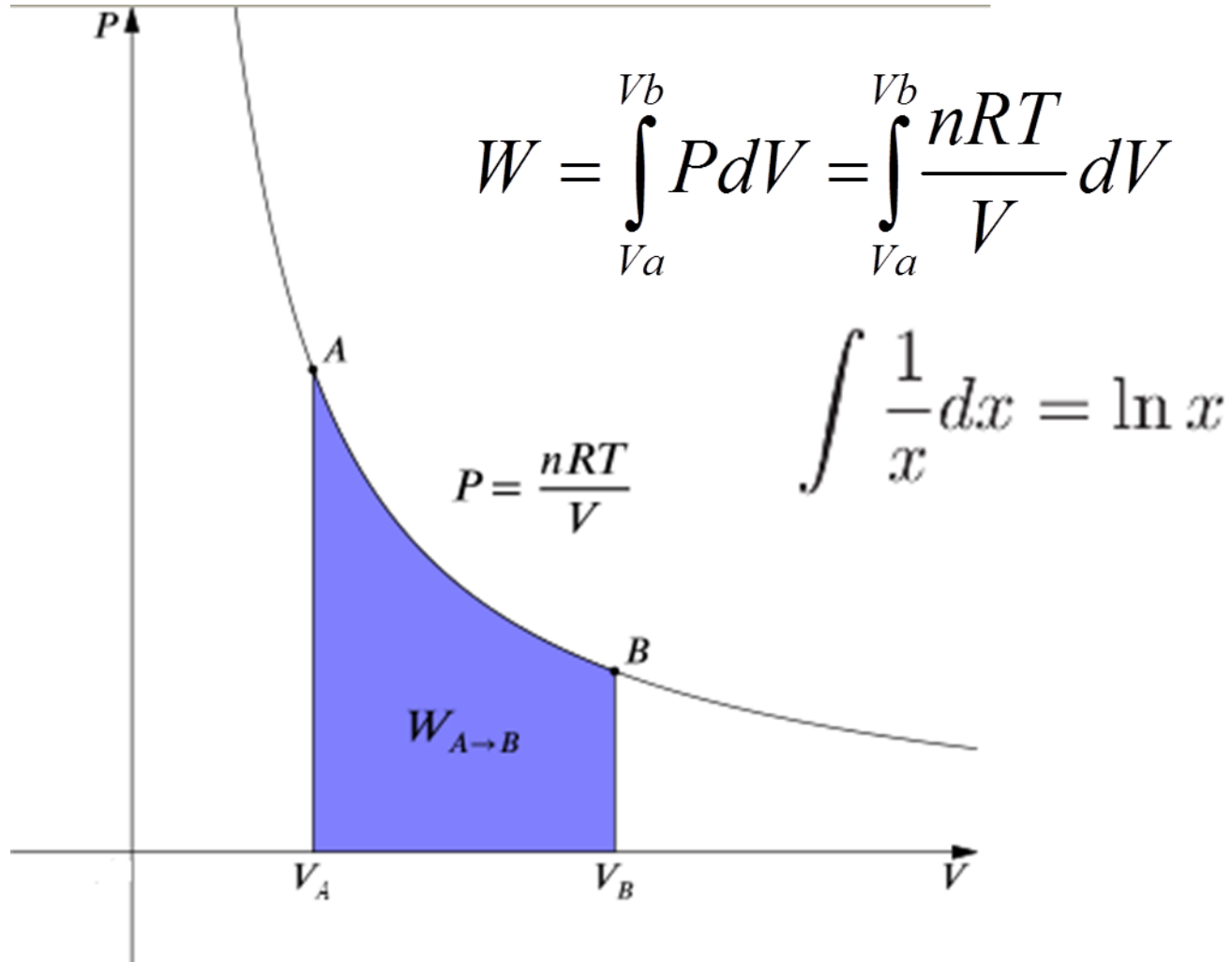
# 1. ZADATAK

- Kojeg volumena trebaju biti spremnici i koliki rad treba uložiti da bi se 1 kg vodika komprimirao, pri sobnoj temperaturi, pod tlakom od:
  - $p_1 = 25 \text{ MPa}$
  - $p_2 = 35 \text{ MPa}$
  - $p_3 = 70 \text{ MPa}$
  - $\rho = 0,00008988 \text{ g/ml}$

# 1. ZADATAK

- $n(\text{H}_2) = \frac{m(\text{H}_2)}{M(\text{H}_2)} = 496 \text{ mol}$
- $V_{\text{atm}}(\text{H}_2) = n(\text{H}_2) \times V_m = 11117 \text{ L}$
- $V_{\text{atm}}(\text{H}_2) = m(\text{H}_2) / \rho(\text{H}_2) = 11126 \text{ L}$
- $V_{20\text{bar}}(\text{H}_2) = \frac{p_{\text{atm}}}{p_{20\text{bar}}} \times V_{\text{atm}} = 563,67 \text{ L}$
- $V_{25\text{MPa}}(\text{H}_2) = \frac{p_{20\text{bar}}}{p_{25\text{MPa}}} \times V_{20\text{bar}} = 45,09 \text{ L}$
- $V_{35\text{MPa}}(\text{H}_2) = \frac{p_{20\text{bar}}}{p_{35\text{MPa}}} \times V_{20\text{bar}} = 32,21 \text{ L}$
- $V_{70\text{MPa}}(\text{H}_2) = \frac{p_{20\text{bar}}}{p_{70\text{MPa}}} \times V_{20\text{bar}} = 16,10 \text{ L}$

# Izotermalna kompresija



# 1. ZADATAK

$$W = nRT \ln(V_b / V_a)$$

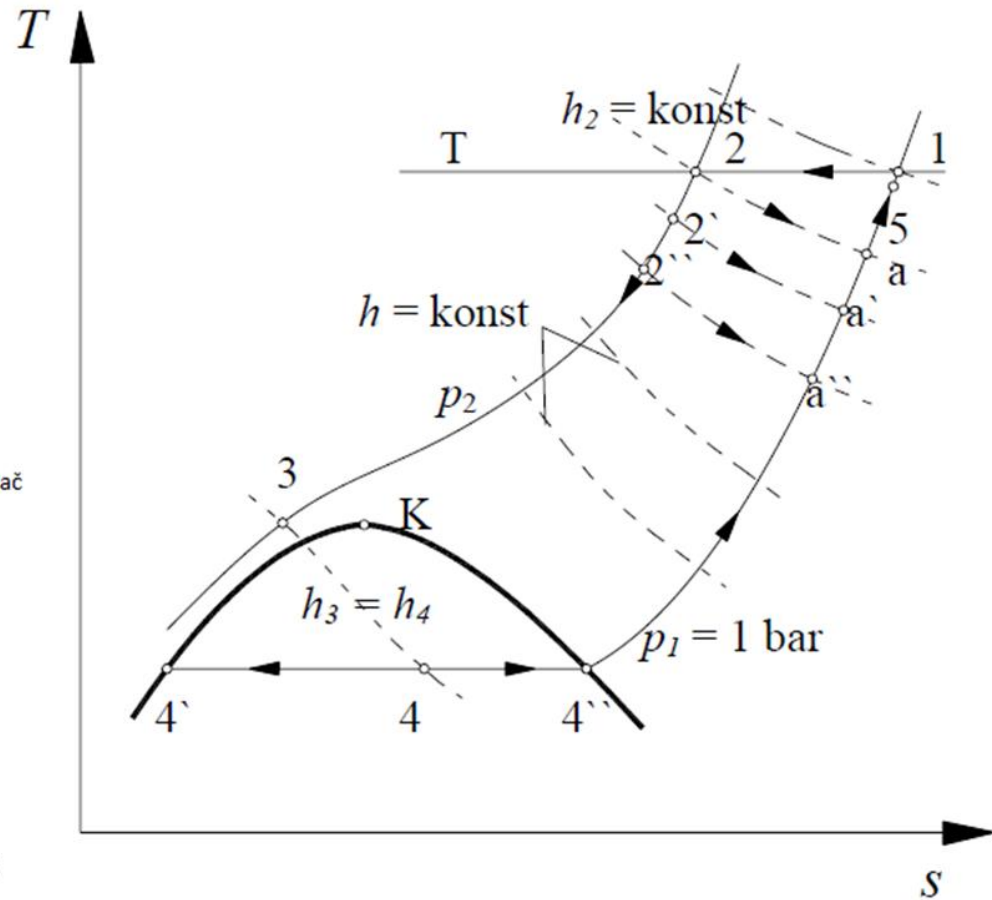
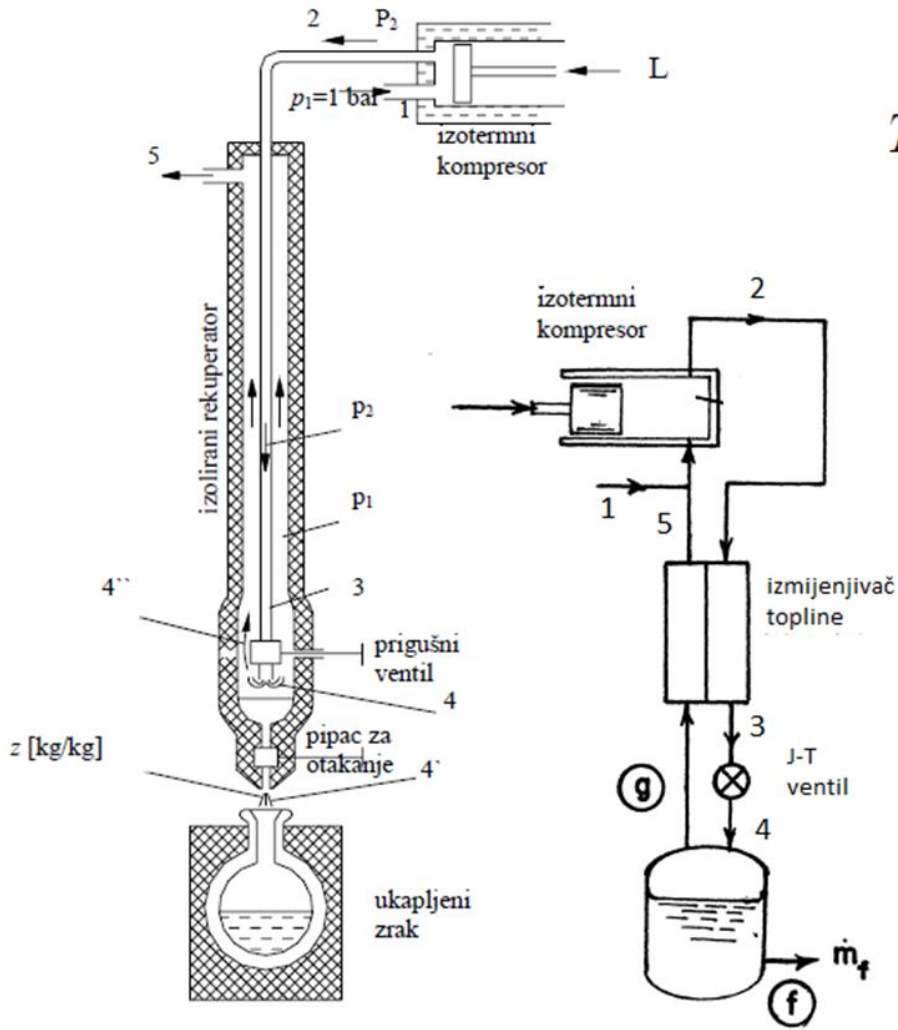
- $W_{\text{atm-}\rightarrow 25} = 1,880 \text{ kWh}$
- $W_{\text{atm-}\rightarrow 35} = 1,995 \text{ kWh}$
- $W_{\text{atm-}\rightarrow 70} = 2,232 \text{ kWh}$
- $W_{20\text{bar-}\rightarrow 25} = 0,862 \text{ kWh}$
- $W_{20\text{bar-}\rightarrow 35} = 0,977 \text{ kWh}$
- $W_{20\text{bar-}\rightarrow 70} = 1,214 \text{ kWh}$



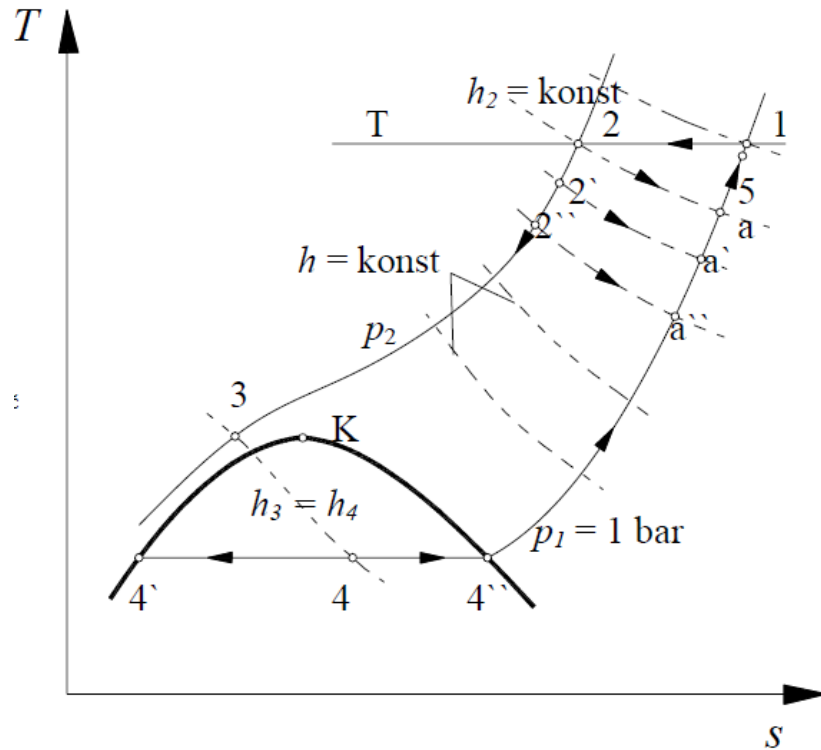
# Tekuci vodik H<sub>2</sub> (l)



# Linde-Hampsonov sustav za ukapljivanje



# T, s - dijagram procesa



- 1-2 izotermna kompresija  $p_1 \rightarrow p_2$
- 2-3 izobarno hlađenje  
 $T_1 \rightarrow T_2$
- 3-4 ekspanzija pri konstantnoj entalpiji  
 $p_2 \rightarrow p_1$
- 4' vrela kapljevina
- 4'' para
- 4-5 izobarno grijanje

$$W = T(s_1 - s_2) - (h_1 - h_2)$$

# Idealno ukapljivanje vodika

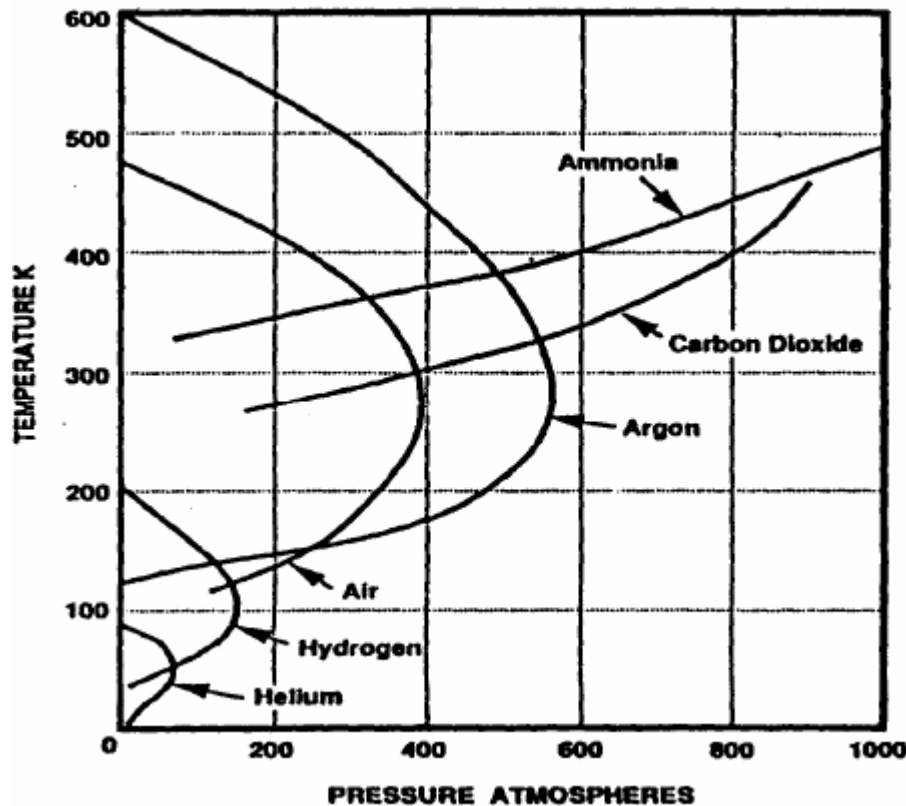
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- $s_1 = 141,29 \text{ J/K mol}$
- $h_1 = 8515,07 \text{ J/mol}$
- $s_2 = 36,69 \text{ J/K mol}$
- $h_2 = 590,15 \text{ J/mol}$
- $T = 300 \text{ K}$
- $W/\text{kg} = 3,232 \text{ kWh/kg}$

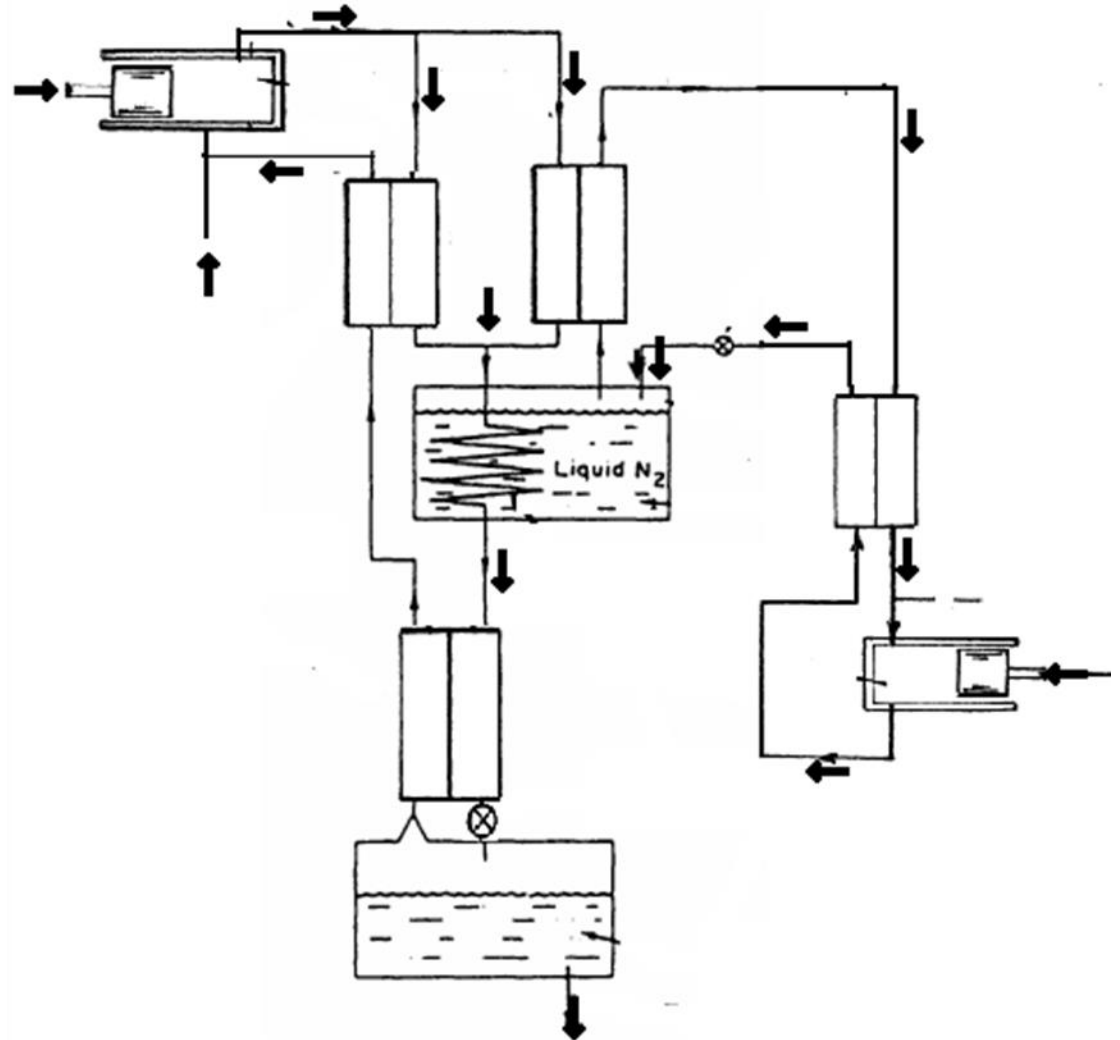
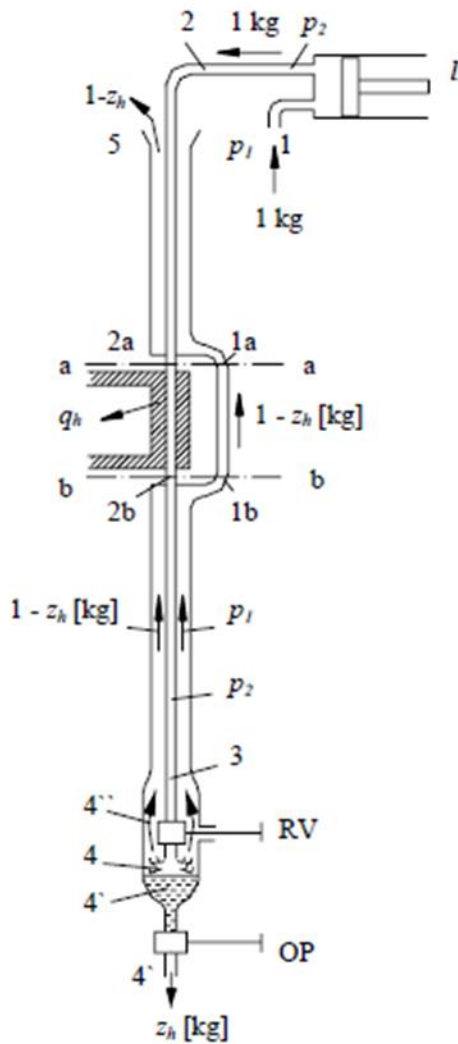
# Joule - Thomsonov prigušni učinak

$$\left( \frac{\Delta T}{\Delta p} \right)_h = \frac{T - T_0}{p - p_0}$$

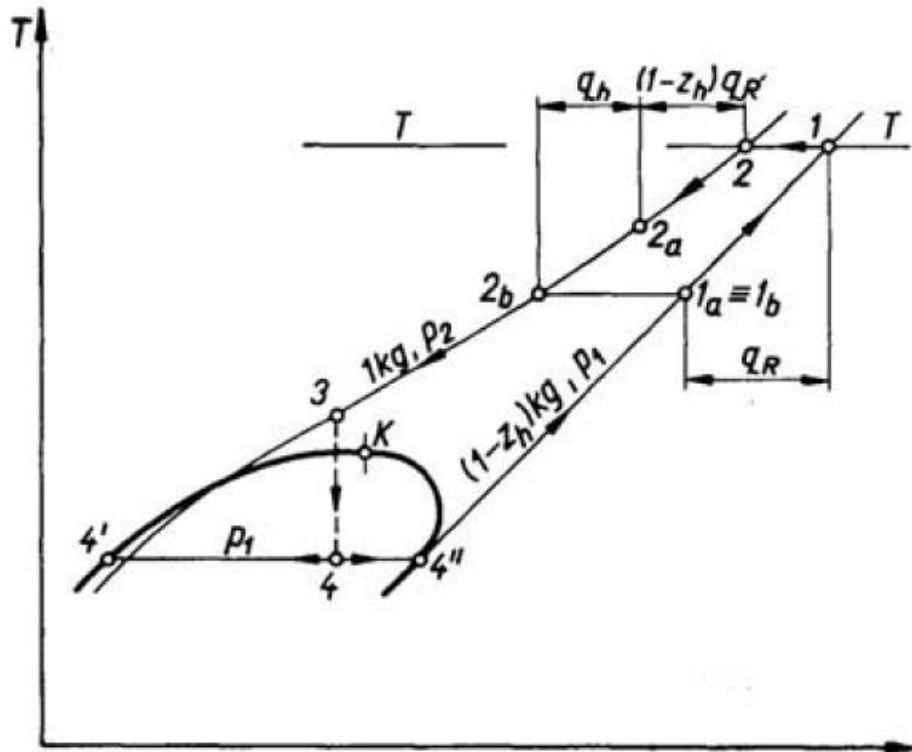
Tvar	$T_K$	$T_{inv0}$
Zrak	132,6	$\approx 760$
H <sub>2</sub>	33,18	$\approx 200$
He	5,19	$\approx 40$



# Predchlázení tekucím dušikom



# T, s - dijagram procesa



- 1-2 izotermna kompresija  $p_1 \rightarrow p_2$
- 2-2<sub>a</sub> izobarno hlađenje  
 $T_1 \rightarrow T_2$
- 2<sub>a</sub>-2<sub>b</sub> snižavanje temperature pomoću rashladnog sredstva-uređaja  $T_2 \rightarrow T_3$
- 2<sub>b</sub>-3 izobarno hlađenje  
 $T_3 \rightarrow T_4$
- 3-4 ekspanzija pri konstantnoj entalpiji  $p_2 \rightarrow p_1$
- 4' vrela kapljevina ; 4'' para
- 4-1 izobarno grijanje

$$W = T(s_1 - s_2) - (h_1 - h_2) + r(T_{N_2}(s_{1N_2} - s_{2N_2}) - (h_{1N_2} - h_{2N_2}))$$

# Ukapljivanje dušika

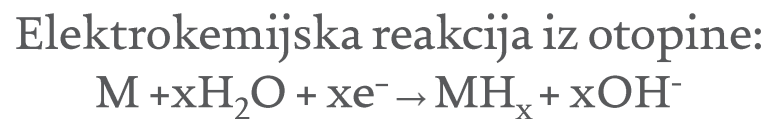
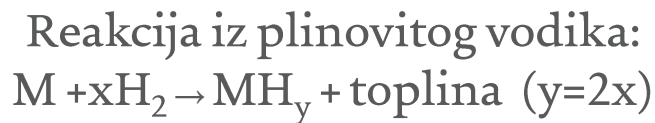
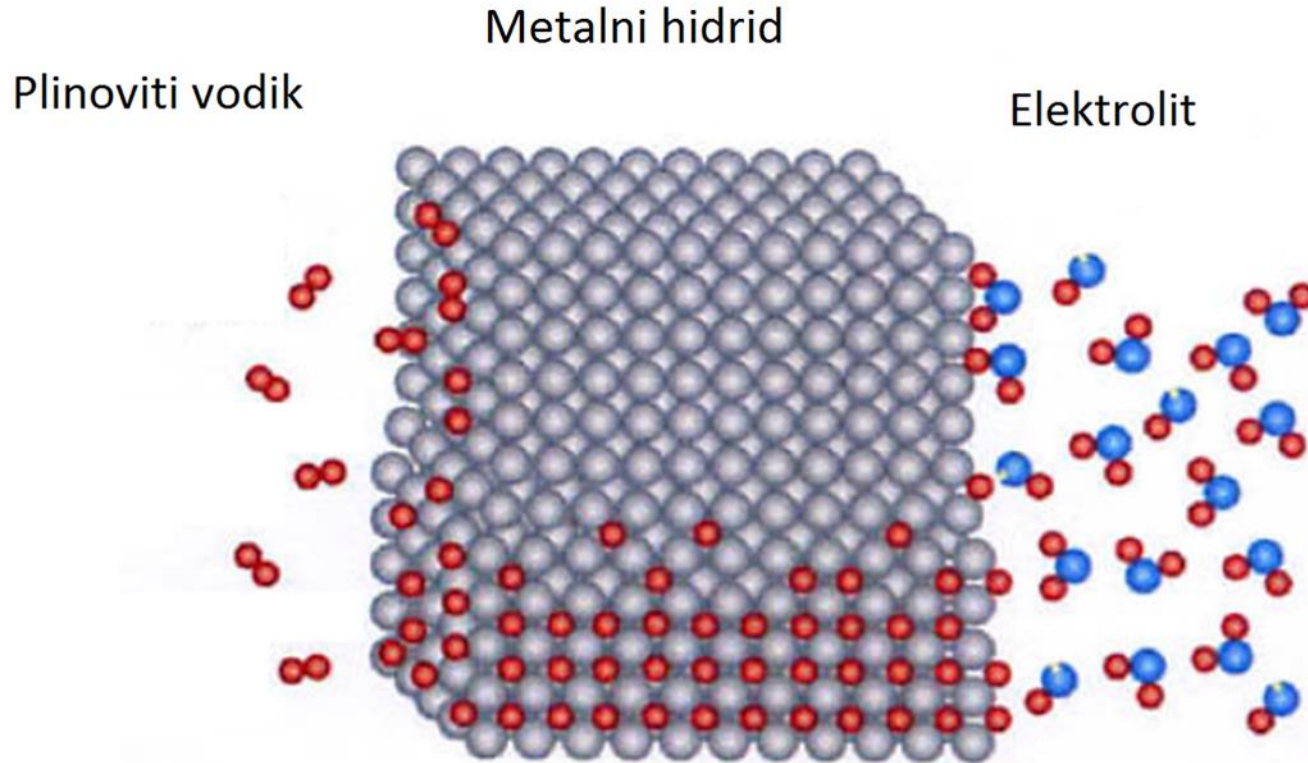
- $s_1 = 4,393 \text{ J/K g}$
- $h_1 = 460 \text{ J/g}$
- $s_2 = 3,033 \text{ J/K g}$
- $h_2 = 445 \text{ J/g}$
- $T = 300 \text{ K}$
- $W_{\text{idealno/kg}} = 0,109 \text{ kWh}$
- $y = 0,09$   $y$  - učinkovitost hlađenja
- $W_{\text{realno/kg}} = 1,211 \text{ kWh}$



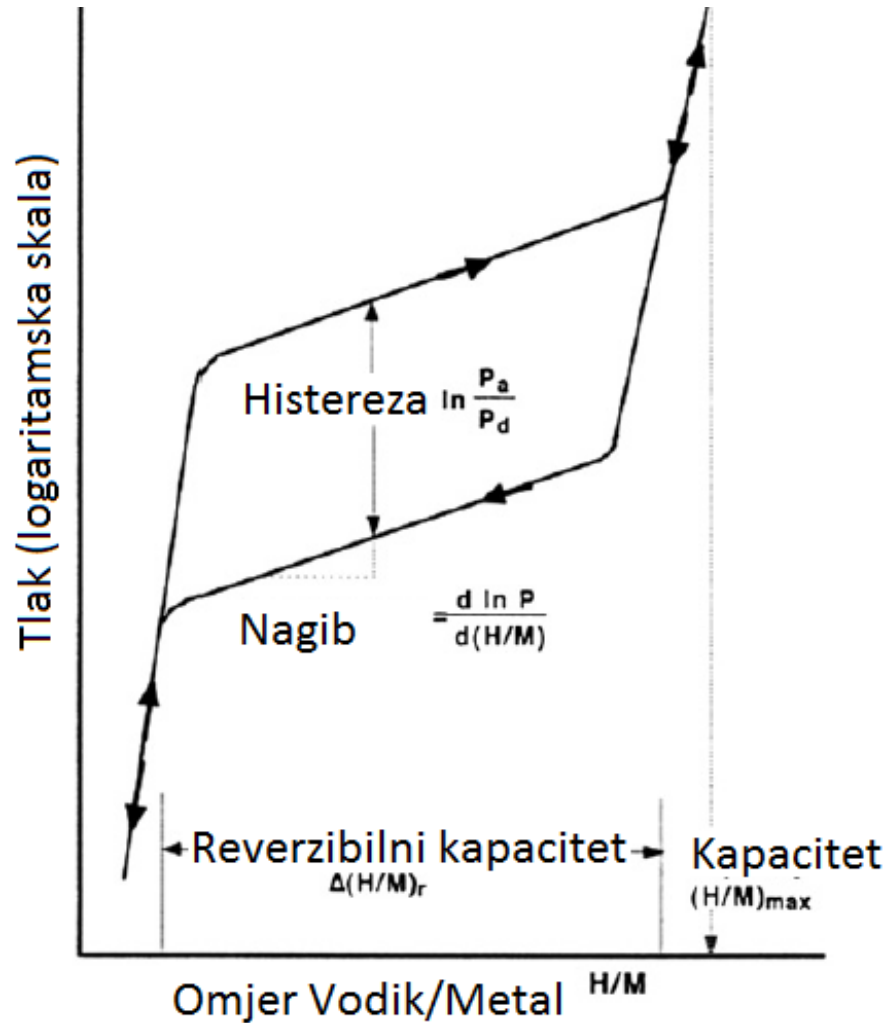
# Ukapljivanje vodika

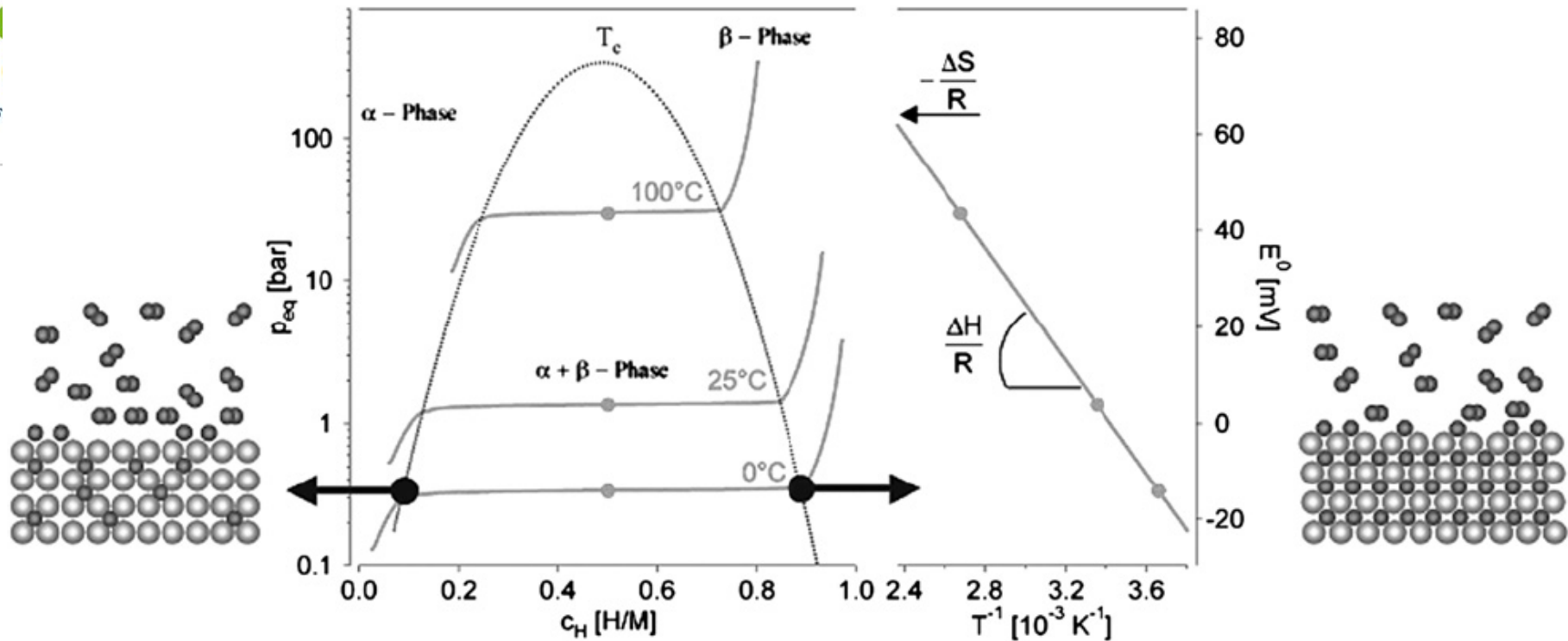
- $W = T(s_1 - s_2) - (h_1 - h_2) + r (T_{N_2} (s_{1N_2} - s_{2N_2}) - (h_{1N_2} - h_{2N_2}))$
- $s_1 = 70,08 \text{ J/K g}$        $h_1 = 4223,75 \text{ J/g}$
- $s_2 = 32,426 \text{ J/K g}$        $h_2 = 4269,72 \text{ J/g}$
- $s_{1N_2} = 4,393 \text{ J/K g}$        $h_{1N_2} = 460 \text{ J/g}$
- $s_{2N_2} = 3,033 \text{ J/K g}$        $h_{2N_2} = 445 \text{ J/g}$
- $T_{H_2} = T_{N_2} = 300 \text{ K}$
- $r = 1; y = 0,081$
- $W_{\text{real/kg}} = 19,778 \text{ kWh}$

# Metalni hidridi



# PCT krivulja (pressure-composition-temperature)





Porastom temperature rastu i ravnotežni tlakovi

Odnos između tlaka i temperature zadan je Van't Hoffovom jednačbom

$$\ln\left(\frac{P_{eq}}{P_{eq}'}\right) = \frac{\Delta H}{R} \cdot \frac{1}{T} - \frac{\Delta S}{R}$$

Dok  $\Delta H$  ovisi o jačini M-H veze i jako varira od metala do metala,  $\Delta S$  je povezan s tranzicijom molekularnog vodika u atomski vodik (plinovita faza u čvrstu) te je gotovo jednak za sve hidride

# Metalni hidridi

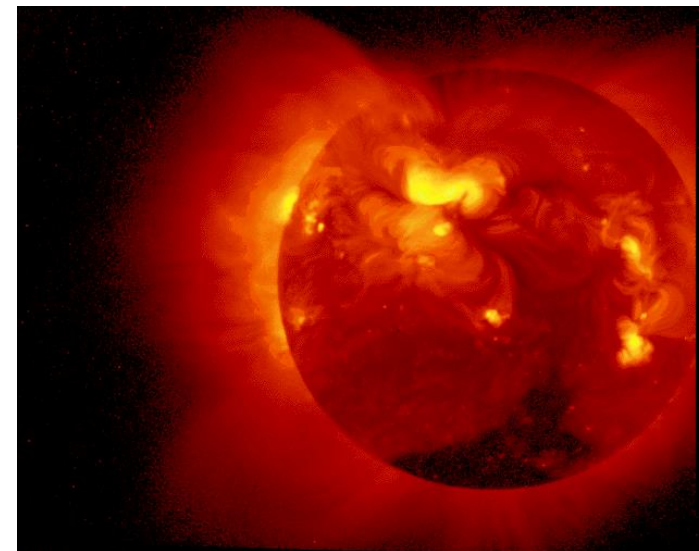
Materijal	Hidrid	Kapacitet (H <sub>2</sub> mas. %)	Pohranjena energija	Entalpija hidrogeniranja
LaNi <sub>5</sub>	LaNi <sub>5</sub> H <sub>6</sub>	1,3	1,850	30,1
TiFe	TiFeH <sub>1,95</sub>	1,7	2,560	28,1
ZrMn <sub>2</sub>	ZrMn <sub>2</sub> H <sub>4</sub>	1,7	2,419	53,2
Mg <sub>2</sub> Ni	Mg <sub>2</sub> NiH <sub>4</sub>	7,0	10,000	64,5
Mg	MgH <sub>2</sub>	7,7	11,000	74,2

$$W_{\text{LaNi}_5} = 4,147 \text{ kWh}$$

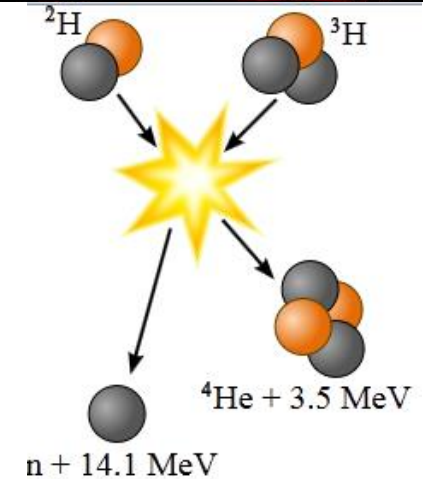
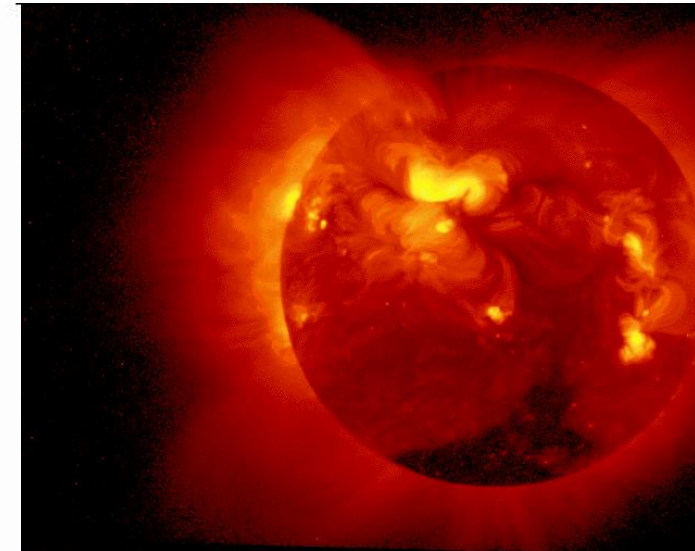
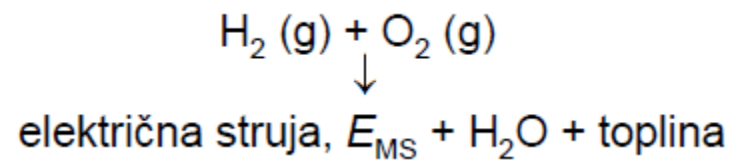
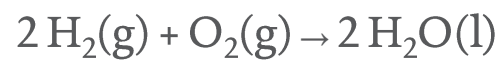
$$W_{\text{Mg}} = 10,22 \text{ kWh}$$



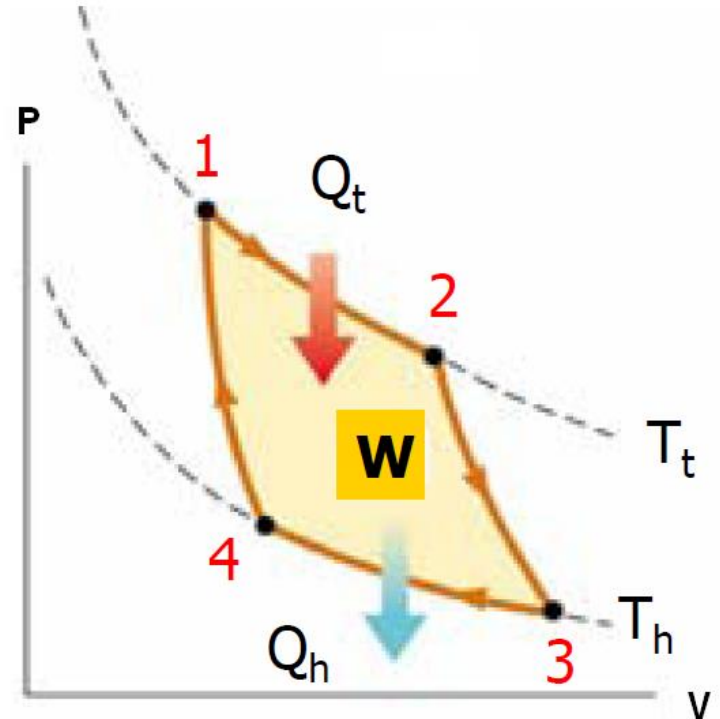
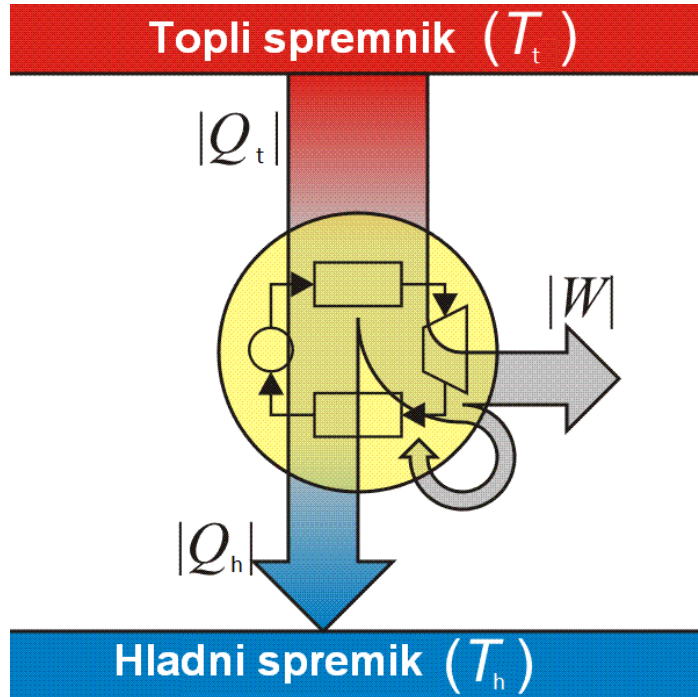
# Primjena vodika



# Mogućnosti primjene vodika



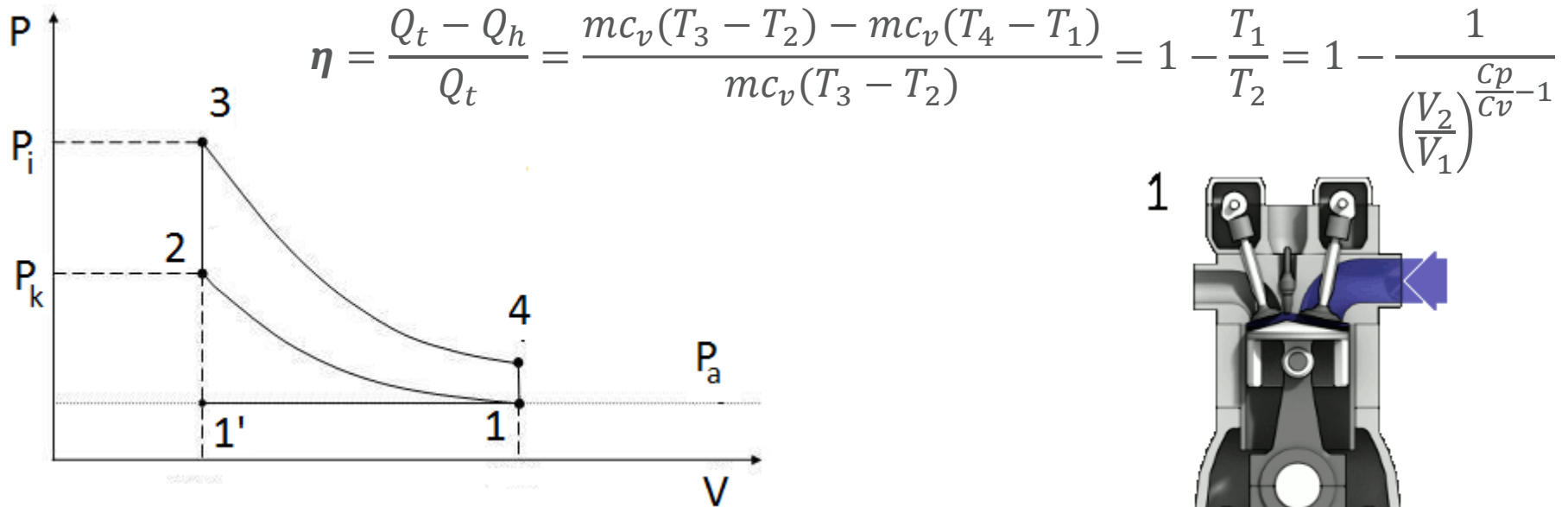
# Toplinski motor – Carnotov ciklus



- 1-2 izotermna ekspanzija
- 2-3 adijabatska ekspanzija
- 3-4 izotermna kompresija
- ⊗ 4-1 adijabatska kompresija



# Motor s unutarnjim izgaranjem



## ○ Četverotaktni Otto motor

- 1. takt 1'-1, usis zraka i plinovitog goriva
- 2. takt 1-2, kompresija i zapaljenje u točki 2
- 3. takt 2-4, 2-3 izgaranje goriva; 3-4 ekspanzija
- 4. takt 4-1', 4-1 pad tlaka na atmosferski; 1-1' ispuh plinova van iz komore

## 2. ZADATAK

- Koliko je iskorištenje Ottovog motora u slučaju da koristimo:
  - Benzin
  - Vodik
 kao gorivo uz pretpostavku da oba sagorijevaju u istom motoru.

$$a) \frac{V_2}{V_1} = 10:1$$

$$b) \frac{V_2}{V_1} = 17:1$$

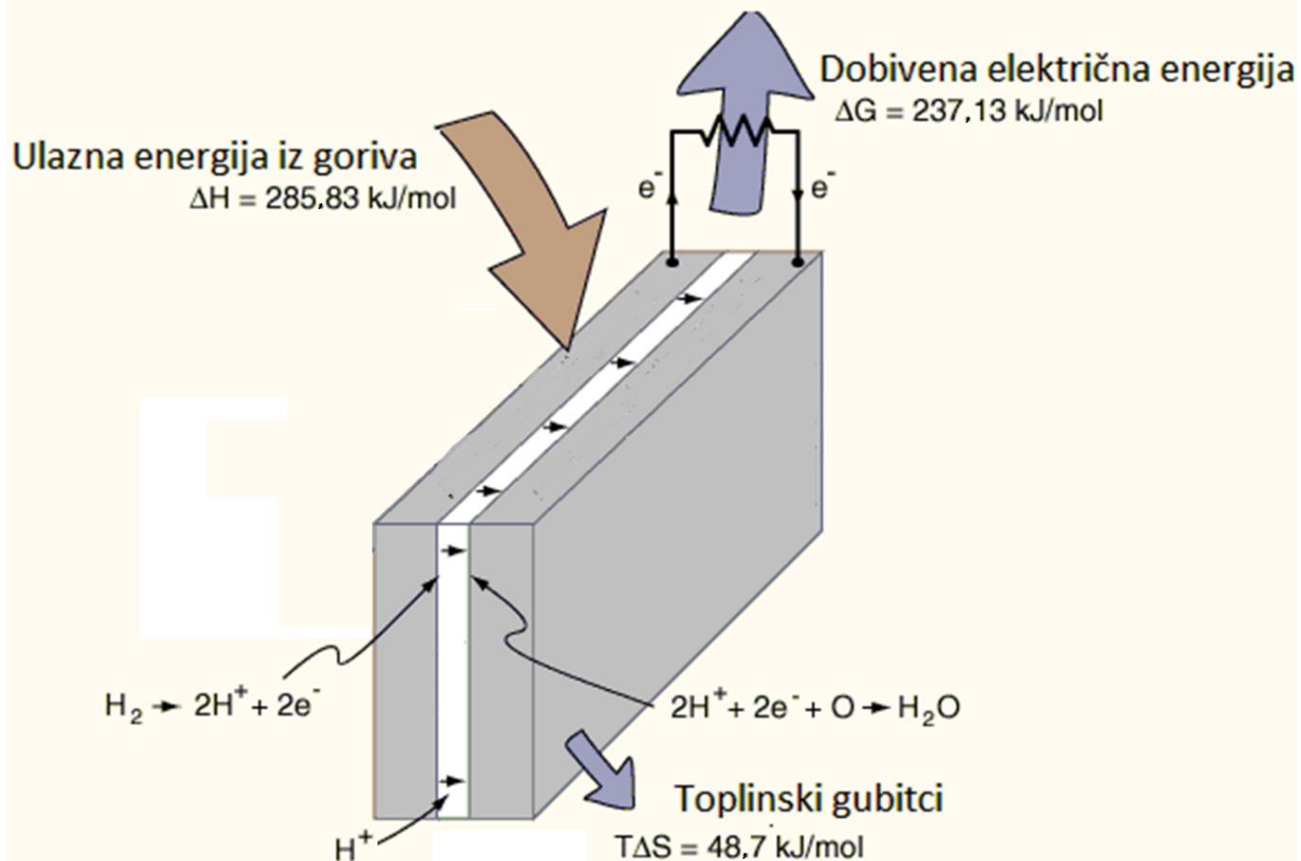


## 2. ZADATAK

- $C_p (H_2) = 14,32 \text{ kJ/kg K}$       $C_v (H_2) = 10,16 \text{ kJ/kg K}$
- $C_p (\text{benzin}) / C_v (\text{benzin}) = 1,1$
- $\eta(H_2) = 1 - \frac{1}{\left(\frac{V_2}{V_1}\right)^{\frac{C_p}{C_v}-1}} = 0,61$
- $\eta(H_2) = 1 - \frac{1}{\left(\frac{V_2}{V_1}\right)^{\frac{C_p}{C_v}-1}} = 0,69$
- $\eta(\text{benzin}) = 1 - \frac{1}{\left(\frac{V_2}{V_1}\right)^{\frac{C_p}{C_v}-1}} = 0,21$
- $\eta(\text{benzin}) = 1 - \frac{1}{\left(\frac{V_2}{V_1}\right)^{\frac{C_p}{C_v}-1}} = 0,25$

# Gorivni članak

## Idealni gorivni članak vodik-kisik



# Idealna učinkovitost / idealni standardni potencial

- A(-):  $\text{H}_2 \rightarrow 2\text{H}^+ + 2\text{e}^-$
- K(+):  $2\text{H}^+ + 2\text{e}^- + \frac{1}{2}\text{O}_2 \rightarrow \text{H}_2\text{O}$
- $\text{H}_2(\text{g}) + \frac{1}{2}\text{O}_2(\text{g}) \rightarrow \text{H}_2\text{O}(\text{l})$
- $\Delta H = (H_{\text{H}_2\text{O}}) - (H_{\text{H}_2} + \frac{1}{2}H_{\text{O}_2}) = -285,83 \text{ kJ/mol}$
- $\Delta S = (S_{\text{H}_2\text{O}}) - (S_{\text{H}_2} + \frac{1}{2}S_{\text{O}_2}) = -163,6 \text{ J/K mol}$
- $\Delta G = \Delta H - T\Delta S = -237,06 \text{ kJ/mol}$
- $\eta_{ideal} = \frac{\Delta G}{\Delta H} = 0,83$
- $E^0 = \frac{\Delta G}{-z \times F} = 1,229\text{V}$  Idealni standardni potencial

# Realna učinkovitost gorivnog članka

$$\eta_{\text{realan}} = \frac{E_{\text{članka}} \times I \times \eta_{\text{ideal}}}{E^0 \times I} = \frac{E_{\text{članka}} \times 0,83}{1,229} = 0,675 \times E_{\text{članka}}$$

